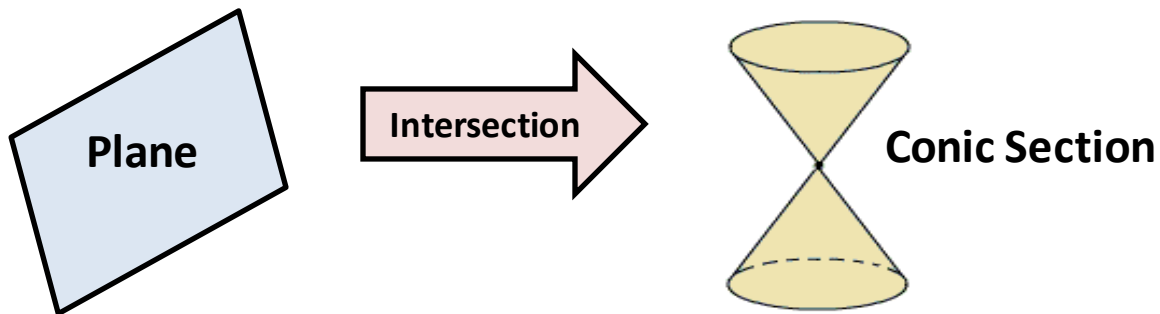


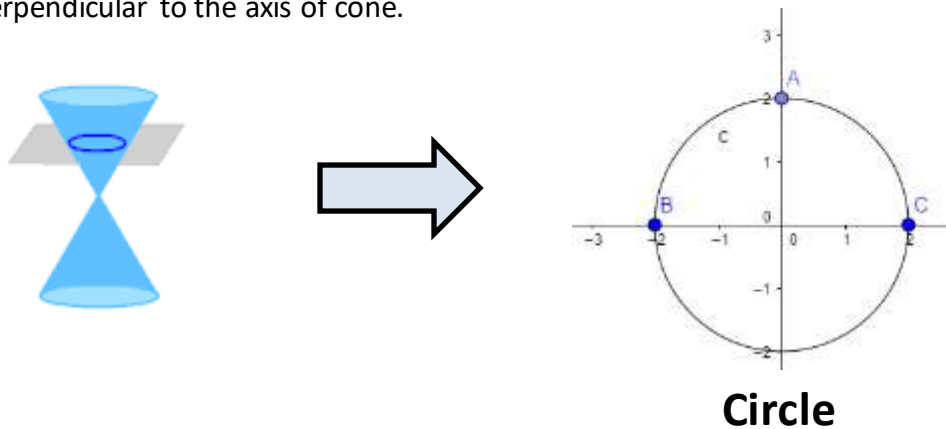
EXPLORING CONIC SECTIONS Guided Notes

A **Conic Section** is a curve formed by the intersection of a plane and a double cone.



By the intersection of this plane and the conic section, we can have a **circle**, an **ellipse**, a **parabola** or a **hyperbola**.

A **Circle** is a curve formed by the intersection of a plane and a double cone such that the plane is perpendicular to the axis of cone.



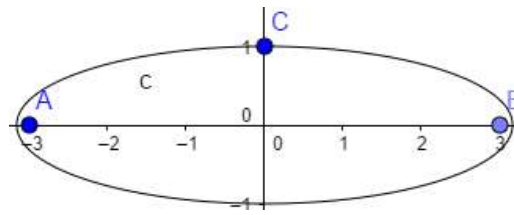
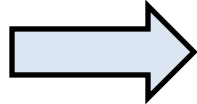
General equation: $(x - h)^2 + (y - k)^2 = r^2$

(h, k) is the center of the circle.

Problem 1: Write the equation of circle whose center is at the origin.

EXPLORING CONIC SECTIONS Guided Notes

An **Ellipse** is a curve formed by the intersection of a plane and a double cone such that the plane cuts the cone at an angle.

**Ellipse**

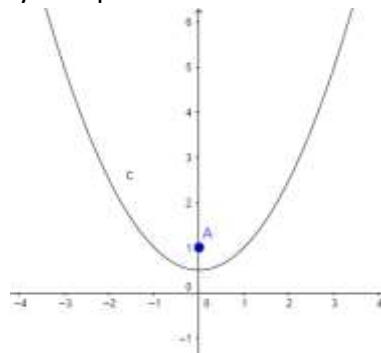
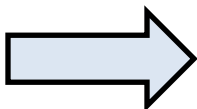
General equations:

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1 \quad \text{(Horizontal Ellipse)}$$

$$\frac{(x-h)^2}{b^2} + \frac{(y-k)^2}{a^2} = 1 \quad \text{(Vertical Ellipse)}$$

Problem 2: Write the equation of a horizontal ellipse whose center is at the origin.

A **Parabola** is a curve formed when the plane cuts any one portion of the double cone at angle.

**Parabola**

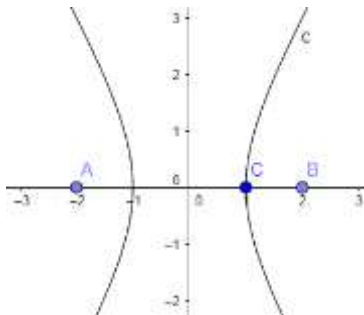
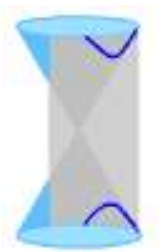
EXPLORING CONIC SECTIONS Guided Notes**General equations:**

$$(y - k)^2 = 4a(x - h) \quad \text{(Horizontal Parabola)}$$

$$(x - h)^2 = 4a(y - k) \quad \text{(Vertical Parabola)}$$

Problem 3: Write the equation of a vertical parabola whose center is at the origin.

A **Hyperbola** is a curve formed when the plane is parallel to the axis of the double cone and cuts both cones.



Hyperbola

General equations:

$$\frac{(x - h)^2}{a^2} - \frac{(y - k)^2}{b^2} = 1 \quad \text{(Horizontal parabola)}$$

$$\frac{(y - k)^2}{a^2} - \frac{(x - h)^2}{b^2} = 1 \quad \text{(Vertical parabola)}$$