

Probability Guided Notes

1. Define probability.

Probability is the likelihood that an event will occur under a set of given conditions. The probability of an event occurring has a value between 0 and 1.

2. How is probability expressed mathematically?

If an event E is defined in a sample space S then its mathematical form is:

$$P(A) = \frac{m}{n} = \frac{\text{Number of samples points in } A}{\text{Number of samples points in } S} = \frac{n(E)}{n(S)}$$

3. Define term 'event' in respect of probability.

An event is an individual outcome or any number of outcomes (sample points) of a random experiment.

4. What is sample place?

A set consisting of all possible outcomes that can result from a random experiment:
e.g. the experiment of tossing a coin results in either of two possible outcomes, a Heads (H) or a Tails (T).

So the sample space for this experiment may be expressed as $S=\{H,T\}$

5. Define Mutually Exclusive Events.

Two events A and B of single experiment are said to be mutually exclusive or disjoint if they cannot both occur at same time.

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A die is rolled find the probability that an odd number is obtained.

The sample space S is

$$S = \{1, 2, 3, 4, 5, 6\}$$

Let E be event of even number

$$E = \{1, 3, 5\}$$

The probability is

$$P(E) = \frac{n(E)}{n(S)} = \frac{3}{6} = \frac{1}{2}$$

Two coins are tossed, find the probability that two Heads are obtained.

The sample space S is given by

$$S = \{(H, T), (H, H), (T, H), (T, T)\}$$

Let E be event that two Heads are obtained

$$E = \{(H, H)\}$$

The probability is:

$$P(E) = \frac{n(E)}{n(S)} = \frac{1}{4}$$

A coin is tossed three times what is the probability that at least one Heads appears?

$$S = \{HHH, HHT, HTH, THH, HTT, THT, TTH, TTT\}$$

$$n(S) = 8$$

Let A be an event that at least one head appears then

$$A = \{HHH, HHT, HTH, THH, HTT, THT, TTH\}$$

$$n(A) = 7$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{7}{8} \approx 0.87$$